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Robust object characterization from lensless microscopy videos

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Abstract—Lensless microscopy, also known as in-line digital holography, is a 3D quantitative imaging method used in various fields including microfluidics and biomedical imaging. To estimate the size and 3D location of microscopic objects in holograms, maximum likelihood methods have been shown to outperform traditional approaches based on 3D image reconstruction followed by 3D image analysis. However, the presence of objects other than the object of interest may bias maximum likelihood estimates. Using experimental videos of holograms, we show that replacing the maximum likelihood with a robust estimation procedure reduces this bias. We propose a criterion based on the intersection of confidence intervals in order to automatically set the level that distinguishes between inliers and outliers. We show that this criterion achieves a bias / variance trade-off. Section IV illustrates the performance of the proposed robust estimation procedure to characterize microscopic objects. Special attention is paid on the setting of the level to distinguish between inliers and outliers. An automatic criterion based on the intersection of confidence intervals is proposed to achieve a bias / variance tradeoff. Section IV illustrates the performance of the proposed method on holographic videos.

I. INTRODUCTION

Thanks to the massive development of low-cost imaging sensors and the simultaneous increase in computational capabilities, lensless microscopy is emerging as a method of choice for time-resolved analysis of microscopic objects. It is already used in several fields where the accurate estimation of 3D location and size over time is crucial, such as in the study of fluid flows or biomedical imaging [1].

Analysis of digital holograms is traditionally performed by first reconstructing the 3D volume by light back-propagation, then analyzing this 3D volume to segment, locate and size objects [2]. However, this approach suffers from artifacts due to the imperfect reconstruction step, in particular to spatial distortions close to the image borders and spurious diffraction patterns known as twin images in holography [2]. Location and size estimates can be significantly improved by using a maximum likelihood estimator, i.e., by fitting a model of the diffraction pattern generated by the object of interest directly on the hologram rather than by reconstructing the image volume. This method is very successful for the study of isolated objects [3], [4], but some bias appears when unwanted objects in the field of view alter the hologram. These objects may have complex or unknown shapes and their influence on the hologram may be difficult to explicitly model and account for.

We suggest replacing the maximum likelihood estimator with a robust estimator so that any notable discrepancies between the model of the pattern of interest and the data due to unwanted objects have less influence on the final estimate. Section II provides a brief presentation of the lensless microscopy principle and the model of the diffraction pattern generated by spherical objects behaving as opaque objects such as droplets, cells or cocci bacteria. Section III then describes the proposed robust estimation procedure to characterize microscopic objects. Special attention is paid on the setting of the level to distinguish between inliers and outliers. An automatic criterion based on the intersection of confidence intervals is proposed to achieve a bias / variance tradeoff. Section IV illustrates the performance of the proposed method on holographic videos.

II. CHARACTERIZATION OF MICROSCOPIC OBJECTS WITH LENSLESS IMAGING

Lensless microscopes are based on the in-line holographic setup originally proposed by Dennis Gabor [5]. The objects are illuminated by an incident monochromatic plane wave of wavelength $\lambda$. After free-space propagation over distance $z_p$, a hologram $d$ is recorded by a monochromatic image sensor, see Fig. 1.

Based on diffraction theory, it is possible to model the diffraction pattern created on the hologram plane by an object of interest of given 3D shape, absorption and optical index. The case of opaque spherical objects is of particular practical interest since it covers opaque particles introduced within the flow in fluid mechanics, and colored spherical objects such as cocci bacteria or cells in flow cytometry in biology. When the distance $z_p$ is such that $z_p \gg \sqrt{\frac{4\pi r^3}{\lambda^2}}$, the diffraction pattern of an opaque sphere located at $(x_p, y_p, z_p)$, with radius $r$, is [6]:

$$m_p(x, y) = \frac{\pi r^2}{\lambda z_p} J_1 \left( \frac{2\pi r_p \rho_p}{\lambda z_p} \right) \sin \left( \frac{\pi \rho_p}{\lambda z_p} \right),$$

where $\rho_p = \sqrt{(x-x_p)^2 + (y-y_p)^2}$ is the transversal distance to the center of the sphere and $J_1(u) = J_0(u)/u$ is the cardinal Bessel function of first order. More generally, in the following $m_\theta(a, b)$ denotes the intensity of the diffraction pattern generated at the pixel location $(a, b)$ on the sensor by an object of interest. This object of interest is fully characterized by a vector of parameters $\theta$ (e.g., for an opaque sphere $\theta = \{x_p, y_p, z_p, r_p, \}$).
Maximum likelihood estimation of the parameters $\theta$ of the object of interest, under the hypothesis of additive white Gaussian noise, amounts to solving a nonlinear least-squares problem [3]:

$$\hat{\theta}^{(ML)} = \arg \min_{\theta} \sum_{a=1}^{A} \sum_{b=1}^{B} w(a,b) \cdot [m_\theta(a,b) - d(a,b)]^2,$$  \hspace{1cm} (2)

where $d(a,b)$ represents the recorded data, $w(a,b) \propto 1/\epsilon(a,b)^2$ is a weight that is set to zero for defective pixels and that can account for a non-stationary noise variance $\epsilon(a,b)^2$, and $A$ and $B$ are the height and width of the sensor, in pixels.

III. PROPOSED ROBUST ESTIMATION SCHEME

A. Robust estimation by reweighted least squares

To reduce the impact of outliers on the estimation, Huber introduced the so-called M-estimators [7] that replace the least squares with weights $w(a,b)$:

$$\hat{\theta}^{(M)} = \arg \min_{\theta} \sum_{a=1}^{A} \sum_{b=1}^{B} w(a,b) \cdot \rho \left( \frac{m_\theta(a,b) - d(a,b)}{s} \right),$$  \hspace{1cm} (3)

where $\rho$ is a non-negative, continuous and symmetric function with a minimum equal to 0 at 0, and $s$ is a parameter that scales the residuals by setting the level that distinguishes between inliers and outliers.

Depending on the choice of the function $\rho$, the minimization problem (3) can be difficult to solve. A simple algorithmic strategy leading to a local minimizer consists in solving a sequence of least-squares problems of the form (2); the Iteratively Reweighted Least Squares (IRLS) [8]. In this scheme, the estimate $\hat{\theta}_{k+1}$ at iteration $k+1$ is obtained by reweighting the squares with weights $w_k(a,b)$ derived from the residuals of iteration $k$:

$$\hat{\theta}_{k+1} := \arg \min_{\theta} \sum_{a=1}^{A} \sum_{b=1}^{B} w_k(a,b) \cdot [m_\theta(a,b) - d(a,b)]^2,$$  \hspace{1cm} (4)

where the weights $w_k(a,b)$ are computed from the residuals $r_k(a,b) = m_\theta(a,b) - d(a,b)$ at iteration $k$ according to an update rule that depends on the objective function $\rho$:

$$w_k(a,b) = w(a,b) \cdot \frac{s}{r_k(a,b)} \cdot \left. \frac{\partial \rho(u)}{\partial u} \right|_{u = r_k(a,b)/s}.$$  \hspace{1cm} (5)

Many different objective functions $\rho$ and their associated weight update rules have been studied and classified in the literature [9]. So-called hard-redescenders are functions $\rho$ that are constant above a given threshold, thereby leading to assign zero weights to data points that display a misfit larger than the chosen threshold. So-called soft-redescenders are functions $\rho$ whose limit at infinity is finite, thus asymptotically producing zero weights for large residual values. For lensless applications, we selected a soft-redescender to achieve a good compromise between bias reduction and loss of efficiency of the estimator. In the following, we use the Cauchy objective function:

$$\rho(u) = \frac{1}{2} \log(1 + u^2),$$  \hspace{1cm} (6)

which gives the following weight update:

$$w_k(a,b) = w(a,b) \cdot \left[ 1 + \left( \frac{r_k(a,b)}{s} \right)^2 \right]^{-1}.$$  \hspace{1cm} (7)

B. Automatic tuning of parameter $s$: distinguishing inliers and outliers

 Adequate tuning of the parameter $s$ is essential in robust estimation schemes [10]. On the one hand, if $s$ is too low, most residuals $r_k(a,b)$ will be (much) larger than $s$ and the weights of the corresponding data points will decrease in the following iteration, thereby discarding most of the signal of interest. In this case, the result will be an increase in the variance of the estimation. On the other hand, if $s$ is too large (much larger than the typical discrepancy of outliers), the M-estimator tends to the least squares estimator and loses its robustness properties. In this case, reduction in the bias caused by outliers is no longer obtained.

A common method to estimate the scale parameter $s$ is based on the median absolute deviation (MAD) estimator, which provides a robust estimate of the residuals standard-deviation [7]:

$$s^{(MAD)} = 1.48 \cdot \text{median} \left[ |r - \text{median}(r)| \right],$$  \hspace{1cm} (8)

where $r$ denotes the collection of all residuals values $r(a,b)$ for $a \in [1,A]$ and $b \in [1,B]$.

MM-estimators have been proposed to achieve high robustness to the presence of outliers while conserving high efficiency in the absence of outliers[11]. These estimators consist in two steps: (i) estimation of the scale of the residuals $s$ using an M-estimator defined by a hard-redescender $\rho$; and (ii) actual estimation of the parameters of interest $\theta$ with a more efficient penalty function $\rho$ (such as a soft-redescender).

One drawback of these methods of setting parameter $s$ is that they do not account for the actual impact of the outliers on the estimation. When considering unwanted objects within the field of view, the location of the objects with respect to the object of interest may or may not lead to biases. In other words, while $s^{(MAD)}$ is suitable in cases where the outliers are uniformly distributed in the measured signal, a more appropriate choice of $s$ could be made in cases of non-uniform distribution of outliers.

We propose to estimate parameter $s$ using a method that accounts for the actual impact of the outliers on the estimation. Starting from the value $s^{(MAD)}$, which may be over-conservative, we apply the intersection of confidence intervals (ICI) rule to decide up to what point parameter $s$ can be
increased to reduce estimation variance before being subject to bias due to outliers. The ICI rule has been successfully applied in image denoising to locally select the largest neighborhoods on which to perform denoising by local polynomial approximation [12]. Its application only requires knowledge of the estimate along with its standard deviation.

The vector of parameters $\theta$ is estimated using the robust IRLS estimation scheme (4) by progressively increasing parameter $s$ until the new estimate $\hat{\theta}_s^{(M)}$ obtained with parameter $s$ leads to a confidence interval $[\hat{\theta}_s^{(M)} - \delta, \hat{\theta}_s^{(M)} + \delta]$ with an empty intersection with the preceding confidence intervals:

$$\hat{s}^{(ICL)} = \max \left\{ s \in \left[ \hat{s}^{(MAD)}, \infty \right) \mid \exists \theta, \forall s_0 \in \left[ \hat{s}^{(MAD)}, s \right], \theta \in \left[ \hat{\theta}_s^{(M)} - \delta, \hat{\theta}_s^{(M)} + \delta \right] \right\}. \tag{9}$$

This principle is illustrated in Fig. 2 considering a single parameter $\theta$.

To build the confidence intervals, we used the Cramér-Rao Lower Bounds (CRLBs) [13]. The CRLB $\delta(i)$ represents the minimum standard-deviation for any unbiased estimator of the parameter $\theta(i)$. Under additive white Gaussian noise, the least squares estimator (2) asymptotically reaches the CRLB given by:

$$\delta^2(i) = \left[ I(\theta)^{-1} \right]_{i,i}, \tag{10}$$

where Fisher information matrix $I$ is defined by:

$$[I(\theta)]_{i,j} = \sum_{a=1}^{A} \sum_{b=1}^{B} w(a,b) \frac{\partial m_{\theta}(a,b)}{\partial \theta(i)} \frac{\partial m_{\theta}(a,b)}{\partial \theta(j)}, \tag{11}$$

In the presence of outliers, we approximate the confidence intervals by computing the CRLB with the weights obtained by the IRLS procedure.

To reduce the computational cost of estimating parameter $s$ according to the ICI rule (9), we consider a non-uniform discretization of the set $[\hat{s}^{(MAD)}, \infty)$ such that two successive $s$ values lead to a given decrease in the CRLBs. In practice, each $s$ value is obtained by bisection to achieve the prescribed CRLBs reduction.

We now illustrate the tuning of parameter $s$ based on the ICI rule (9) on a simple 1D problem: estimating the $x_p$ location of a Gaussian-shaped pattern $m$. We simulate 100 noisy realizations $d$ by adding to the model a Gaussian white noise (with a peak signal-to-noise ratio of 10) and a constant outlier formed by a rectangular function with 3 samples in width (with a peak signal-to-noise ratio of 1), see Fig. 3(a).

The ICI rule leads to values of $s$ that are about 5 times larger than $\hat{s}^{(MAD)}$ when the outlier is too far to introduce a significant bias, and to values of $s$ close to that of $\hat{s}^{(MAD)}$ when the outlier affects the estimation, see Fig. 3(b). When $\hat{s}^{(ICL)}$ is higher than $\hat{s}^{(MAD)}$ (resulting in a weaker penalization of the residuals), the mean square error (MSE) on the location of the pattern is reduced by a factor between 2 and 4. In practice, the empirical standard-deviation reaches the CLRB when the outlier has little impact on the estimate. A difference of a few tens of percent is observed when the constant outlier has an impact on the estimate since the estimator is no longer asymptotically unbiased. Determination of $s$ with an ICI rule is still possible. In conclusion, choosing the parameter $s$ with the ICI rule improves the mean square error compared to a MAD estimator.

IV. APPLICATION TO LENSELESS MICROSCOPY VIDEOS

In this section, the performance of the robust estimate scheme applied in lensless microscopy is evaluated on two lensless imaging applications. The goal is to accurately estimate the radius $r_p$ of spherical objects. We also evaluate the performance of a robust estimation performed jointly over several consecutive frames (super-resolution). In these examples, the image formation model $m_{\theta}$ is non-linear with respect to the parameters $\theta$, as given by equation (1). As a result, the minimization problem (2) and each IRLS iteration in (4) is solved using a few iterations of Levenberg-Marquardt algorithm. The original videos and the results of the robust estimation are available online at http://perso.univ-st-etienne.fr/denioloic/robust_lensless_video.html.

A. Holographic video of an object of constant size

We consider a 200 frames video of a slightly moving particle located near an unwanted object. The object of interest...
is a circular chromium deposit on a glass plate, with a calibrated radius of 50 µm (Optimask™, diameter ± 1 µm, roundness error ± 0.25 µm). The unwanted object is a fixed human hair [14].

Since the outlier is fixed throughout the video, it is possible to roughly remove outlier pixels by applying a static binary weighting mask \( w(a, b) = 0 \) if pixel \((a, b)\) is in the masked region, \( w(a, b) = 1 \) otherwise. Figure 4 shows two frames from the video and the manual removal of the outlier by masking. Due to the mask \( w \), part of the signal due to the particle of interest (diffraction rings) is not accounted for.

In each frame the vector of parameters \( \theta \) is estimated by least squares fitting, Eq. (2), with constant weights (hereafter denoted \( \text{single – without mask} \)) or with the binary mask (denoted \( \text{single – with mask} \)), and using the robust M-estimator, Eq. (4) and \( \hat{s}^{(\text{MAD})} \) (denoted \( \text{single – robust} \)). In the case of a joint estimation, the term \( \text{single} \) is replaced by the term \( \text{joint} \) in the denomination of the methods tested.

Figure 4 is an example of the weights used for the last IRLS iteration. The weights are close to a segmentation of the pixels impacted by the unwanted object. The diffraction rings characterizing the particle of interest are well preserved (weights close to 1). Figure 5 shows the evolution of the estimated radius during the IRLS iterations for the first 5 frames of the video. This shows that the algorithm converges in a few iterations and that the joint estimate of the radius carried out by super-resolution is very close to the ground truth equal to 50 µm.

Table I lists the mean estimated radius \( \langle \hat{r}_p^{(M)} \rangle \), the corresponding standard-deviation \( \sigma \) and the CRLB \( \delta \) obtained with \( \hat{s}^{(\text{MAD})} \) for each method tested. The manual removal of the outliers appears to reduce the estimation bias. The bias is further reduced when a robust weighting of residuals by IRLS is applied since it preferentially eliminates the outliers while retaining the signal of interest. As a result, the estimation using a robust approach leads to a very small increase in CLRB which is negligible compared with the reduction of the bias.

The combination of a robust estimation method with a super-resolution scheme (\( \text{joint – robust} \)) exploiting the information redundancy between different frames significantly reduce the estimation standard-deviation. In agreement with statistical results [15], we observed a decrease in the standard-deviation by a factor at least equal to \( \sqrt{5} \). This joint robust estimation approach enables accurate (i.e. low bias and low standard-deviation) estimates of the radius of the holographic objects and thus improves the overall performance of a conventional least squares estimation process.

**B. Holographic video of evaporating droplets**

We used a 160 frames video of an evaporating diethyl ether droplet dispersed in a homogeneous and nearly isotropic turbulence that is tracked over time. As the particle evaporates, it produces a plume of vapor that diffuses around it. The vapor plume creates outliers since its signal mixes with the signal produced by the particle of interest. Other evaporating particles passing close to the particle of interest also act as outliers. The evaporation rate of these particles was recently studied using the least squares approach (2) [16].

Figure 6(b) shows two frames from the video and the 2D trajectory of the particle over time (superimposed color line). Figure 6(a) shows the evolution of the restate factor of the residuals obtained with a MAD estimator and with the proposed ICI rule as well as the IRLS weights for two different frames. The ICI rule leads to a larger value of \( s \) than MAD but without notably modifying the estimation of the radius \( r_p \). This is the case when outliers do not disturb the estimate like in frame 60 (left column) since the particle of interest is isolated and the plume of vapor is rather small. In contrast, \( \hat{s}^{(\text{MAD})} \) and \( \hat{s}^{(\text{ICI})} \) are very close when the particle of interest is strongly disturbed by outliers. This is illustrated by frame 97 (right...
column) where another evaporating particle is close to the particle of interest and disturbs its signal. These observations underline the fact that the MAD estimator only accounts for the presence of outliers strongly deviating from the model but does not account for their spatial localization and hence, their actual impact on the estimate. Figure 6(c) illustrates the evolution of confidence intervals for increasing values of $s$. Figure 6(d) shows the weights obtained at the end of the IRLS procedure for $\hat{s}_{\text{MAD}}$ (first row) and $\hat{s}_{\text{ICI}}$ (second row). On frame 60, $\hat{s}_{\text{ICI}}$ is significantly larger than $\hat{s}_{\text{MAD}}$, leading to larger weights, while on frame 97 $\hat{s}_{\text{MAD}} = \hat{s}_{\text{ICI}}$ and the weights are identical.

Figure 7 shows the evolution of the estimated radius over time with the three methods of estimation tested. The robust estimation scheme leads to an average increase of about 90% of the maximum efficiency obtained without reweighting.

V. CONCLUSION

We have shown that the use of a robust approach to estimate the 3D position and size of objects in lensless microscopy videos reduces the estimation bias caused by unwanted objects. We proposed a simple method to estimate the scale parameter that distinguishes between inliers and outliers in the robust estimation scheme. This method is based on an intervals confidence intersection rule and achieves a better bias / variance trade-off than the usual MAD rule. Finally, we have shown that the combination of the proposed robust approach with a joint estimation scheme also reduces the standard-deviation of the estimation and consequently improves the overall performance of the method.

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